Abstract: By studying the properties of a billiard ball bouncing around a square table, we will be led to the ergodic theory of flows on surfaces, the Gauss circle problem for counting lattice points, and the study of continued fractions.